

Simplify the rational expression, if possible.

9.
$$\frac{x^2 - x - 20}{x^2 + 2x - 15} = \frac{(x-5)(x+4)}{(x+5)(x-3)}$$

10.
$$\frac{x^2 + 6x}{x^2 + 8x + 12} = \frac{x(x+6)}{(x+6)(x+2)} = \frac{x}{x+2}$$

Perform the indicated operation and simplify.

11.
$$\frac{80x^4}{y^3} \cdot \frac{xy}{5x^2} = \frac{16x^3}{y^2}$$

12.
$$\frac{3x^2y}{4x^3y^5} \div \frac{6y^2}{2xy^3} = \frac{3x^2y}{4x^3y^5} \cdot \frac{2xy^3}{6y^2} = \frac{1}{4y^3}$$

Find the least common multiple.

13. $x^4 - 4x^2$ and $x^2 - 2x - 8$
 $x^2(x^2-4)$ $(x-4)(x+2)$
 LCD: $x(x-4)(x+2)(x-2)$

14. $2(x+3)$ and $x(x^2+10x+21)$
 $2x-6$ and x^3+10x^2+21x
 LCD: $2x(x+3)(x+7)$

Perform the indicated operation and simplify.

15. $\frac{2}{3x} + \frac{7}{4x}$ LCD: $12x$

$$= \frac{2(4) + 7(3)}{12x} = \frac{29}{12x}$$

16. $\frac{x}{x^2-4} - \frac{3x-5}{x^2+4x+4}$ LCD: $(x+2)^2(x-2)$

$$= \frac{x(x+2) - (3x-5)(x-2)}{(x+2)^2(x-2)} = \frac{-2x^2 + 13x - 10}{(x+2)^2(x-2)}$$

Solve the equation.

17. $\frac{3x-3}{x+6} = \frac{3x-3}{2x-1}$
 $3x^2 - 9x + 3 = 3x^2 + 15x - 18$
 $3x^2 - 24x + 21 = 0$
 $3(x^2 - 8x + 7) = 0$ $x=7, 1$
 $3(x-7)(x-1) = 0$

18. $\frac{x+3}{2-2x} = \frac{x^2+x}{1-x}$ LCD: $2(1-x)$
 $x+3 = 2(x^2+x)$
 $x+3 = 2x^2+2x$
 $0 = 2x^2+x-3$
 $x = -3/2$

19. $\frac{2x+14}{x+4} - 2 = \frac{2x+20}{2x+8}$ LCD: $2(x+4)$

20. $\frac{3x}{x+1} = \frac{12}{x^2-1} + 2$ LCD: $(x+1)(x-1)$

$2(2x+14) - 2(2(x+4)) = 2x+20$
 $4x+28-4x-16 = 2x+20$
 $-8 = 2x$
 $x = -4$ no solution

$3x(x-1) = 12 + 2x^2 - 2$
 $3x^2 - 3x = 12 + 2x^2 - 2$
 $x^2 - 3x - 10 = 0$
 $(x-5)(x+2) = 0$
 $x = 5, -2$