

Week 4            Monday 9 September  
Chapter Six:      More Geometry  
Topic:            3.4 The Area of a Triangle  
Lesson Obj:      Students will find the area of a triangle using the sine formula

Review and Intro:

0.      Vocab on board: cosine rule. Homework questions.
1.      Review quiz
2.      When do we use what rules?
3.      How do we find the area of a triangle?

Core Lesson:

4.      How do we find the area of a triangle when we don't have base and height?
5.      Worksheet Problem 1

Check for Understanding:

6.      Students complete worksheet
7.      Complete 126:5-7 in class

Assignment:      Students will study for a test on Trigonometry

Evaluation:

$$A = \frac{1}{2} ab \sin C$$

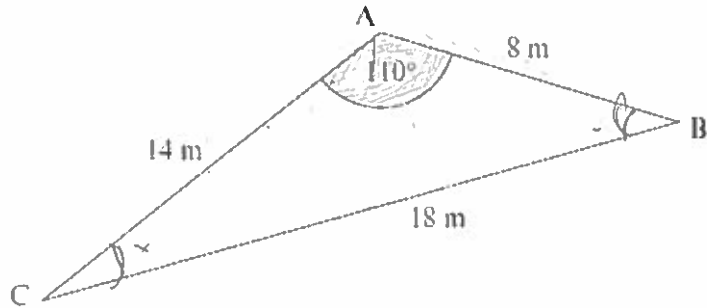
3.4 Area of a Triangle

1. The following diagram shows a triangle ABC. Calculate:

a) the area of triangle ABC.

$$A = \frac{1}{2} (14)(8) \sin 110$$

$$\text{Area} = 52.6 \text{ m}^2$$



b) the size of angle ACB.

$$\frac{18}{\sin(110)} = \frac{8}{\sin(x)}$$

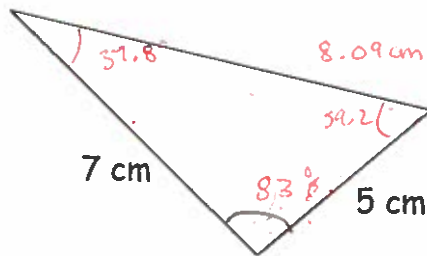
$$24.605$$

$$24.6^\circ = \text{ABC}$$

2. The area of this triangle is 17.4 cm<sup>2</sup>. Find all its sides and angles.

$$17.4 = \frac{1}{2} (7)(5) \sin(x)$$

$$83^\circ = x$$



$$\cos(83) = \frac{7^2 + 5^2 - x^2}{2(7)(5)}$$

$$8.530 =$$

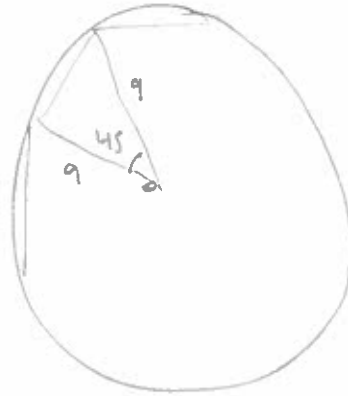
$$-65.47 = -x^2$$

$$8.09 \text{ cm}$$

$$\frac{\sin(83)}{8.09 \text{ cm}} = \frac{\sin(4)}{7 \text{ cm}}$$

$$59.2^\circ$$

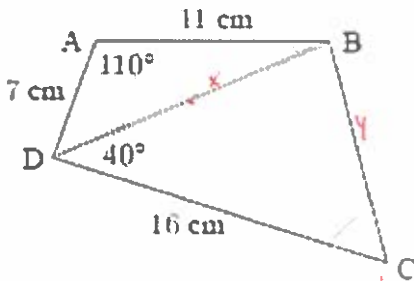
3. Find the area of a regular octagon inscribed in a circle of radius 9 inches.



$$\frac{360}{8} = 45$$

$$A = \left( \frac{1}{2} (9)(9) \sin 45 \right) \cdot 8$$

4. Find the area of the quadrilateral below.



$(\frac{1}{2})^2$

$$\cos(110) = \frac{11^2 + 7^2 - c^2}{11 \cdot 7}$$

$$-0.34202$$

$$-222.66 = c^2$$

$$-222.671 = c^2$$

$$14.9 = x$$

$$\left(\frac{1}{2}\right) \cdot 14.9$$

$$\left(\frac{1}{2}\right) \cdot 7 \cdot 11 \cdot \sin(110)$$

$$9.899$$

$$\left(\frac{1}{2}\right) \cdot 14.9 \cdot 16 \cdot \sin(40)$$

$$76.62$$

$$86.52 = A$$

$$\cos(40) = \frac{16^2 + 14.9^2 - 7^2}{16 \cdot 14.9}$$

$$\cos(40) = \frac{478.671 - 49}{477.504}$$

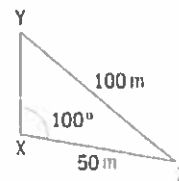
$$365.78 =$$

$$r \cdot 12.881$$

$$10.6 = y$$

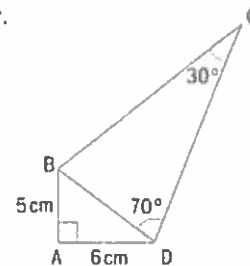
EXAM-STYLE QUESTIONS

- 5 The diagram shows a triangular field XYZ.  
XZ is 50 m, YZ is 100 m and angle X is  $100^\circ$ .



- Find angle Z.
- Find the area of the field. Give your answer correct to the nearest  $10 \text{ m}^2$ .

- 6 The area of an isosceles triangle ABC is  $4 \text{ cm}^2$ . Angle B is  $30^\circ$  and  $AB = BC = x \text{ cm}$ .



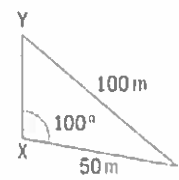
- Write down, in terms of  $x$ , an expression for the area of the triangle.
- Find the value of  $x$ .

- 7 In the diagram,  $AB = 5 \text{ cm}$ ,  $AD = 6 \text{ cm}$ ,  $\hat{B}AD = 90^\circ$ ,  $\hat{B}CD = 30^\circ$ ,  $\hat{B}DC = 70^\circ$ .

- Find the length of DB.
- Find the length of DC.
- Find the area of triangle BCD.
- Find the area of the quadrilateral ABCD.

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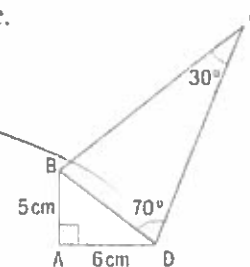


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