

If $s = 1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \frac{1}{16} + \frac{1}{32}$ and $t = 1 + \frac{1}{2}s$, then t exceeds s by

$$\frac{32}{32} + \frac{16}{32} + \frac{8}{32} + \frac{4}{32} + \frac{2}{32} + \frac{1}{32}$$

$$s = \left(\frac{32}{32} + \frac{31}{32} \right) = \frac{63}{32} = \frac{128}{64}$$

$$\begin{aligned} t &= 1 + \frac{1}{2} \left(\frac{63}{32} \right) \\ &= 1 + \frac{63}{64} = \frac{127}{64} \end{aligned}$$

$$80 + 40 + 20 + 10 + 5 + \dots$$

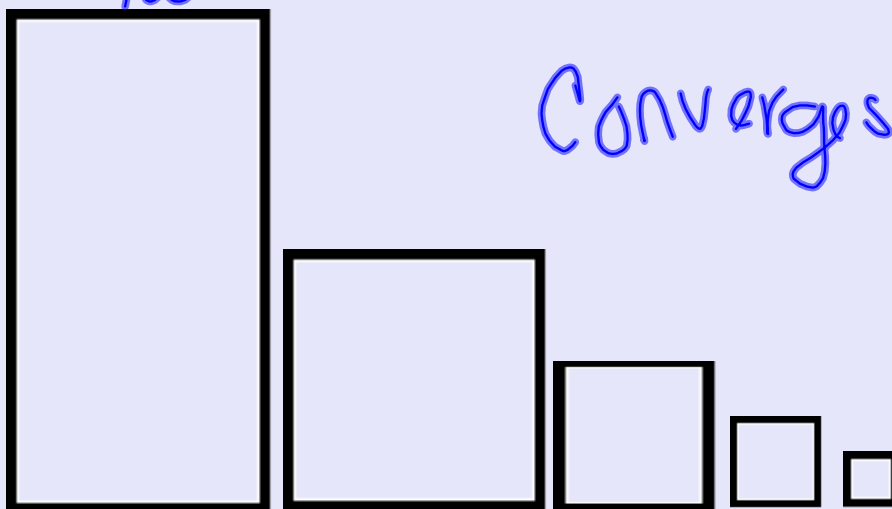
$$S_5 = 155$$

$$S_{10} = 159.8$$

$$S_{100} = 160$$

$$S_n = \frac{80 \left(\frac{1}{2}^n - 1 \right)}{\left(\frac{1}{2} - 1 \right)}$$

Converges @ 160

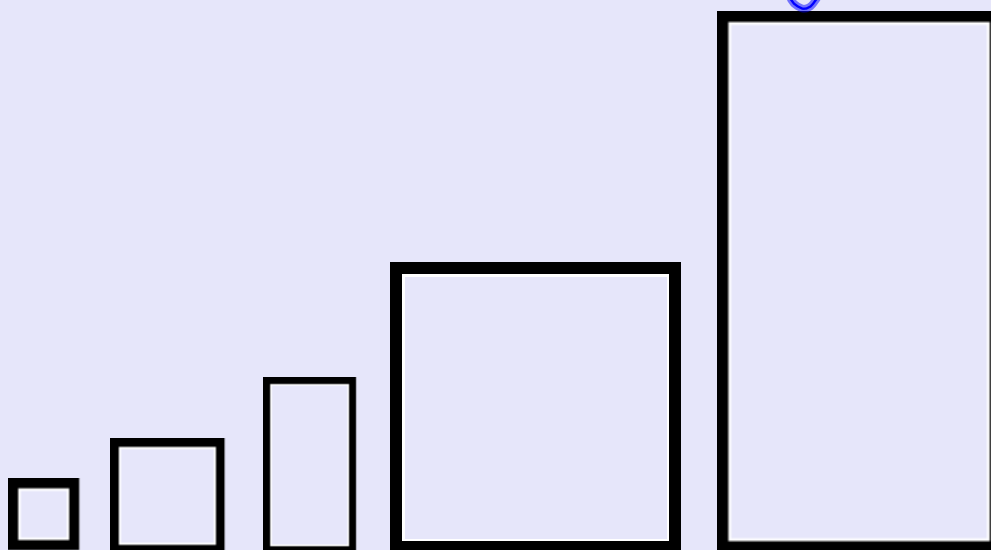


$$5 + 10 + 20 + 40 + 80 + \dots$$

$$S_5 = 155$$

$$S_{10} =$$

Diverges...



$$192 + 48 + 12 + 3 + \dots$$

$$r = \frac{1}{4}$$

$$a_1 = 192$$

$$n = ?$$

$$S_{\infty} = \frac{a_1}{1-r}$$

$$S_{\infty} = \frac{192}{1-\frac{1}{4}}$$

$$= \boxed{256}$$

$$20 - 10 + 5 - 2.5 + 1.25 - \dots$$

$$a_1 = 20$$

$$r = -\frac{1}{2}$$

$$n = \infty$$

$$S_{\infty} = \frac{a_1}{1-r}$$

$$= \frac{20}{1 + \frac{1}{2}} = 13.3$$

The n^{th} term of an
arithmetic sequence

$$u_n = u_1 + (n-1)d$$

The sum of n terms of
an arithmetic sequence

$$S_n = \frac{n}{2}(2u_1 + (n-1)d) = \frac{n}{2}(u_1 + u_n)$$

The n^{th} term of a
geometric sequence

$$u_n = u_1 r^{n-1}$$

The sum of n terms of a
finite geometric sequence

$$S_n = \frac{u_1(r^n - 1)}{r - 1} = \frac{u_1(1 - r^n)}{1 - r}, \quad r \neq 1$$

The sum of an infinite
geometric sequence

$$S = \frac{u_1}{1 - r}, \quad |r| < 1$$

$$\frac{1}{25} + \frac{1}{250} + \frac{1}{2500} + \dots$$

Find the infinite sum.

$$a_1 = \frac{1}{25}$$
$$r = \frac{1}{10}$$

$$S_{\infty} = \frac{2}{45}$$

Write in sigma notation.

$$\sum_{i=1}^{\infty} \frac{1}{25} \left(\frac{1}{10}\right)^{i-1}$$

